

# Asymmetries of information

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# Introduction

## Preamble

- Asymmetries of information : so what?
- Simple economic relation :
  - “seller-buyer” who create a surplus when trading. Very general :
    - cooperation
    - co-financing
    - ...
- When symmetric info : “market” is efficient, whatever the “market power”
- When asymmetric info
  - the surplus of “trade” depends on some “variable” which is private info of one part
  - Problem : how to share it?
  - The way it is managed can generate “market failure” : incentive to cheat, lack of confidence, lack of “effort”...

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- Chapter 0 : reminders of perfect info and introduction to asymmetries
  - a simple economic relation
  - market and market power
  - the “efficiency” theorem
  - The different types of asymmetries of information
    - private info/hidden action
    - examples in economics
    - examples in finance : probability of success of an investment, insider information in a stock market
- Chapter 1 : Lemons
  - The simple model and market shutdown
  - Incentive compatibility
  - Application 1 : in corporate finance : project financing
  - Conclusion

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  - general framework with private value : the delegation model or the seller/buyer model
  - Applications :
    - non linear pricing
    - others...
- Chapter 3 : The theory of incentives : variations and exercises
  - Timing
  - Outside options
  - Common value : the case of insurance
  - Bid-ask spread in market finance
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  - Application to pricing
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  - An example in Corporate Finance
- Chapter 6 : the standard Moral hazard model
  - trade off insurance/incentive
  - Limited liability/Risk aversion
- Chapter 7 : Application to insurance
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# Reminders

- buyers : willingness to pay (bid)  $v_i, v_1 > v_2 > v_3 > v_4 \dots > v_B$
- sellers floor prices (ask)  $c_j, c_1 < c_2 < c_3 < \dots c_S$ .
- Gain from trade  $(i, j)$ :  $v_i - c_j$  if it is positive (surplus).
- How to trade?
  - First solution maximize the sum of surpluses.
    - Optimal trades are those involving buyers and sellers whose index  $(i$  and  $j)$  are lower than

$$k^* = \sup [k, v_k \geq c_k]$$

- market with “auctioneer” :
  - $p$  such that the number of seller that agree is equal to the number of buyers that agree

$$\# \{i, v_i \geq p\} = \# \{j, c_j \leq p\}$$

Main result : the two solutions give the same total surplus and the same trades! (but not the same distribution of surpluses)

## Theorem

*The competitive equilibrium maximizes the total surplus*



# Intuitions

- Take one seller with valuation  $c$  and one buyer with valuation  $v$ .
- In symmetric info the result is “efficient” whatever the bargaining process and the market powers
- Bargaining
  - One move (take or leave)
    - market power (MP) : the one that proposes (the other accepts or refuses). Equilibrium :  $p = v$  (seller has the MP)  $p = c$  (buyer has the MP)
  - Alternating proposals with discounting
    - The Equilibrium surplus sharing is :  $(1 - \alpha)(v - c) = \delta\alpha(v - c)$  that is  $\alpha = \frac{1}{1+\delta}$  : the seller proposes  $p = c + \frac{1}{1+\delta}(v - c)$
- What happens when asymmetric information?

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- What happens when asymmetric information?

- Then if MP and information is not in the same hands there is a problem
- For instance the seller has imperfect info on  $v$  : he cannot set  $p = v$  (since he does not know  $v$ )
- What can he do?
- For instance he has some prior distribution probability on  $v$  :  
$$F(z) = \Pr\{v \leq z\}$$
- He can try to maximize the “expected profit” :  $\max(p - c)(1 - F(p))$

The result will not be efficient

# Chapter 1 : The lemons problem (Akerlof 1970)

- Market for used cars :
  - Two types of used cars H and L, ex ante proportions :  $\lambda_H, \lambda_L$  such that  $\lambda_H + \lambda_L = 1$
  - Market structure : the seller proposes and the buyer accepts or refuses
- Values : bids :  $v_H > v_L$  , asks :  $c_H > c_L$  with  $v_H > c_H$  and  $v_L > c_L$
- Complete symmetric info : everybody knows the  $v$ 's and the  $c$ 's : two markets.

- The equilibrium is

$$p_i^* = v_i, i = H, L$$

All the sellers sell.

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- Incomplete symmetric info :
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$$p^* = \lambda_H v_H + \lambda_L v_L$$

All the sellers sell...and we obtain the same total surplus!



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# Chapter 1

- Asymmetric information : sellers know quality, buyers do'nt
  - What happens if  $c_H > \lambda_H v_H + \lambda_L v_L$ ?
- If the buyer expects that the probability to face a H car is  $\lambda_H$  then he is ready to pay at most  $v = \lambda_H v_H + \lambda_L v_L$ .
  - But this is not enough to satisfy a H seller. This max price is lower than his min price! So that a H seller does not show. He does not want to sell.
  - So it was not rational to expect there is a positive probability to face a H type!
- However it is rational for the buyer to expect that he faces a L seller. Indeed if so the maximal price is  $v_L$  which is lower than  $c_H$  but larger than  $c_L$  : only L sellers are ready to sell at that price!

## Definition

This is Adverse Selection!

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# Chapter 1 Application to Corporate Finance

Project financing :

- An investment (amount  $I$ ) (a project) needs to be integrally financed (no initial cash).
- The return is  $R$  with probability  $p$  and 0 with probability  $(1 - p)$ .
- There are two types of borrowers :  $p_H > p_L$  with ex-ante probabilities  $\alpha$  and  $(1 - \alpha)$  . One sets :  $m = \alpha p_H + (1 - \alpha)p_L$
- Contract : the lender lends  $I$  and leaves  $R_b$  to the borrower in case of success and 0 in case of failure

Fact

*The good projects are creditworthy :  $p_H R \geq I$*

More over we assume perfect competition among lenders and a zero risk-free interest rate :

Fact

*The expected profit of the lender is equal to zero*

# Chapter 1 Application to Corporate Finance

Perfect information benchmark : two different markets

Perfect competition among lenders implies that on each market the expected profit must be 0 :

$$p_i (R - R_b^i) = I$$

That implies that good projects are financed with

$$R_b^H = \frac{p_H R - I}{p_H} \geq 0$$

There are two cases :

- 1 The bad project is not creditworthy ( $p_L R < I$ ), and then is not financed
- 2 The bad project is creditworthy and is financed with

$$0 \leq R_b^L = \frac{p_L R - I}{p_L} < R_b^H$$

# Chapter 1 Application to Corporate Finance

Asymmetric information : one market

Recall we have :

$$p_L R < mR < p_H R$$

Perfect competition among lenders implies that on that market the expected profit must be 0 :

$$m(R - R_b) = I$$

There are three cases :

- ①  $p_L R < mR < I < p_H R$  : complete adverse selection, no financing!
- ②  $p_L R < I \leq mR < p_H R$  : both projects are financed. There is overinvestment since L is not credit worthy. That means there is crosssubsidy : good projects indirectly finance badones.
- ③  $I \leq p_L R \leq mR < p_H R$  : both projects are financed.

In the two last cases :  $R_b^L < R_b < R_b^H$  : the loan is more expensive (the compensation  $R_b$  is lower) for good projects when information is asymmetric

# Chapter 1 Application to Corporate Finance

Application :market timing : negative stock price reaction for a deepening investment



## Chapter 2 The theory of incentive : basic model

- The model :
  - A principal wants to delegate a task to an agent, for example produce  $q$ .
  - The gross surplus achieved by the principal is  $v(q)$  when  $v$  is a strictly increasing concave function with  $v(0) = 0$
  - The cost for the agent is  $c(q) = \theta q$  with  $\theta \in \{\theta_L, \theta_H\}$  (two potential types with resp prob  $\lambda_L, \lambda_H = 1 - \lambda_L$  )
  - Hence the total surplus is  $\sum_i \lambda_i (v(q_i) - \theta_i q_i)$ , this is maximized for  $q_i^*$  such that  $v'(q_i^*) = \theta$
  - The “contract” stipulates the quantity  $q$  to produce and the monetary transfer from principal to agent  $t$

## Chapter 2 The theory of incentive : basic model

- The complete info benchmark
  - The principal observes  $\theta$  : the optimal contract solves :

$$\max_{(t,q)} \{v(q) - t, t - \theta q \geq 0\}$$

$t - \theta q \geq 0$  is called the "Participation Constraint of type  $\theta$ ". Here the outside option is assumed to be 0.

- At the optimum  $t - \theta q = 0$  (obvious). This implies that the problem becomes :

$$\max_q \{v(q) - \theta q\}, t = \theta q$$

That is :

$$v'(q_i^*) = \theta_i$$

$$t_i^* = \theta_i q_i^*$$

## Chapter 2 The theory of incentive : basic model

- Asymmetric information :
  - The principal does not observe the value of  $\theta$ .
  - He proposes a menu of contract :  $\{(t_L, q_L), (t_H, q_H)\}$  , and let the agent choose.
  - Obviously, if the contract chosen by H is different of the one chosen by L, without loss of generality, we call  $(t_i, q_i)$  the one chosen by i.
- Consider first the menu formed by the two complete info contracts  $\{(t_L^*, q_L^*), (t_H^*, q_H^*)\}$ 
  - One has :  $t_H^* - \theta_L q_H^* = (\theta_H - \theta_L) q_H^* > 0 = t_L^* - \theta_L q_L^*$
  - And :  $0 = t_H^* - \theta_H q_H^* > (\theta_L - \theta_H) q_L^* = t_L^* - \theta_H q_L^*$

## Chapter 2 The theory of incentive : basic model

- So that both types chose the H contract! The surplus of the agents are 0 for H and  $(\theta_H - \theta_L) q_H^*$  for L
  - The surplus of the principal is  $v(q_H^*) - \theta_H q_H^*$
- The principal can do better :

## Chapter 2 The theory of incentive : basic model

- By choosing the contract  $(t_H^*, q_H^*)$  the L type obtains a positive surplus equal to  $(\theta_H - \theta_L) q_H^*$ . This is an informational rent.
  - To induce the agent to choose  $(t_L, q_L^*)$  instead (and then to produce more) he must be given a bonus on the top of the cost :

$$t_L = t_L^* + (\theta_H - \theta_L) q_H^*$$

- By doing so, the principal induces L to choose  $(t_L^* + (\theta_H - \theta_L) q_H^*, q_L^*)$ .
  - Then the production is increased, with the same surpluses given to the agent (0 if H,  $(\theta_H - \theta_L) q_H^*$  if L)
- The principal can do even better :

## Chapter 2 The theory of incentive : basic model

- The general program is :

$$\max_{\{(t_H, q_H), (t_L, q_L)\}} \{ \lambda_L (v(q_L) - t_L) + \lambda_H (v(q_H) - t_H) \}$$

- Under the constraints :

$$\begin{aligned} t_L - \theta_L q_L &\geq t_H - \theta_L q_H && IC(L, H) \\ t_H - \theta_H q_H &\geq t_L - \theta_H q_L && IC(H, L) \\ t_L - \theta_L q_L &\geq 0 && PC(L) \\ t_H - \theta_H q_H &\geq 0 && PC(H) \end{aligned}$$

## Chapter 2 The theory of incentive : basic model

- Lemmas
- Lemma 1 : at the optimum  $t_H - \theta_H q_H = 0$  : the transfer is equal to the cost for bad type
- Lemma 2 : at the optimum :  $t_L - \theta_L q_L = t_H - \theta_L q_H$  : the IC(L,H) constraint is binding.
  - Lemma 1 and lemma 2 imply that  $t_L = \theta_L q_L + (\theta_H - \theta_L) q_H$  : there is an information rent (bonus)
- Lemma 3 :  $q_H \leq q_L$
- Lemma 4 : Lemma 1 and lemma 2 and lemma 3 imply that at optimum  $t_H - \theta_H q_H > t_L - \theta_H q_L$  and  $t_L - \theta_L q_L > 0$
- So that the program reduces to :

## Chapter 2 The theory of incentive : basic model

$$\max_{\{q_H, q_L\}} \left\{ \lambda_L (v(q_L) - \theta_L q_L) + \lambda_H \left( v(q_H) - \theta_H q_H - \frac{\lambda_L}{\lambda_H} (\theta_H - \theta_L) q_H \right) \right\}$$

Under the constraint :

$$q_H \leq q_L$$

The payments are given by :

$$t_H = \theta_H q_H$$

$$t_L = \theta_L q_L + (\theta_H - \theta_L) q_H$$



## Chapter 2 The theory of incentive : basic model

Solution :

$$v'(q_L) = \theta_L \Rightarrow q_L = q_L^*$$

$$v'(q_H) = \theta_H + \frac{\lambda_L}{\lambda_H} (\theta_H - \theta_L) \Rightarrow q_H < q_H^*$$

Remark (shut down policy) :  $q_H$  can be 0 if  $\theta_H + \frac{\lambda_L}{\lambda_H} (\theta_H - \theta_L) \geq v'(0)$  i.e

$$\text{if : } \frac{\lambda_L}{\lambda_H} \geq \frac{v'(0) - \theta_H}{\theta_H - \theta_L}$$

## Chapter 3 The theory of incentive : extension

Timing : assume that the timing is the following

- 1 the principal proposes a menu
- 2 The agent accepts or refuses the menu
- 3 The agent learns the value of  $\theta$
- 4 The agent chooses the contract and the chosen contract is executed

### Theorem

*In the case of reverse timing, the principal can obtain the perfect info allocation, if the agent is risk neutral :*

Indeed he proposes for instance :

$$(t_H = v(q_H^*) - T, q_H^*), (t_L = v(q_L^*) - T, q_L^*)$$

This menu verifies IC for all  $T$  !

## Chapter 3 The theory of incentive : extension

Then the principal fixes  $T$  so as to bind the ex-ante participation constraint :

$$\lambda_H(t_H - \theta_H q_H^*) + \lambda_L(t_L - \theta_L q_L^*) \geq 0$$

That leads to :

$$T = \lambda_H(v(q_H^*) - \theta_H q_H^*) + \lambda_L(v(q_L^*) - \theta_L q_L^*)$$

which is the perfect info surplus!

## Chapter 5 The theory of Moral Hazard : An example

- An entrepreneur has a project that needs  $I$  (investment) to start. He has an amount of initial cash equal to  $A$ .
  - So that  $I - A$  must be borrowed.
- The project
  - can succeed : the return is  $R$
  - of fail : the return is 0.
- The entrepreneur can
  - behave (make an effort) and then the project has a probability  $p_H$  to succeed
  - Or he can misbehave (make no effort) and then the project has a probability to succeed equal to  $p_L$ ,
    - and the entrepreneur gets a private benefit  $B$ .

## Chapter 5 The theory of Moral Hazard : An example

- A financing contract specifies the amount borrowed , here  $I - A$  , and the sharing of the return  $R_b$  for the borrower and  $R_\ell$  for the lender.

Assumptions :

$p_H R - I > 0$  the net value is positive when effort

$p_L R - I + B < 0$  the net value is negative when no effort

- These hypothesis mean that the entrepreneur would behave if he financed the project on his own.

Assumption : there is competition among lenders (0 expected profit) :

$$pR_\ell = I - A$$

## Chapter 5 The theory of Moral Hazard : An example

- Incentive constraint (the sharing contract induces that effort is better):

$$p_H R_b \geq p_L R_b + B$$

That is :

$$R_b \geq \frac{B}{\Delta p}$$

So that :

$$R_\ell \leq R - \frac{B}{\Delta p}$$

- This implies

$$p R_\ell - (I - A) \leq p_H \left( R - \frac{B}{\Delta p} \right) - (I - A)$$

## Chapter 5 The theory of Moral Hazard : An example

- The project can be financed if

$$p_H \left( R - \frac{B}{\Delta p} \right) \geq I - A$$

- That is

$$A \geq p_H \frac{B}{\Delta p} - (p_H R - I) = \bar{A}$$

- Interesting when  $\bar{A} \geq 0$  that is  $p_H \frac{B}{\Delta p} \geq (p_H R - I)$ 
  - In that case the project to be financed, needs an amount  $\bar{A}$  of self financing

### Theorem

*When  $A < \bar{A} = p_H \frac{B}{\Delta p} - (p_H R - I)$ , there is credit rationing : one lends only to the rich.*

## Chapter 5 The theory of Moral Hazard : An example

- The continuous case :
- now the return is  $R$  in case of succes, the private benefit is  $B$

Assumptions :

$$p_H R \geq 1$$

$$p_L R + B < 1$$

$$p_H R < 1 + p_H \frac{B}{\Delta p}$$

- The third one means that the net expected revenue is less than the expected information rent.



## Chapter 5 The theory of Moral Hazard : An example

- The incentive constraint becomes :

$$p_H R_b \geq p_L R_\ell + BI$$

- That is

$$R_b \geq \frac{BI}{\Delta p}$$

- Then for the lender :

$$R_\ell \leq \left( R - \frac{B}{\Delta p} \right) I$$

- So that

$$p_H R_\ell - (I - A) \leq P_H \left( R - \frac{B}{\Delta p} \right) I - (I - A)$$

## Chapter 5 The theory of Moral Hazard : An example

- In order to be financed (expected profit  $\geq 0$ ) : we must have :

$$\frac{I}{A} \leq \frac{1}{1 - P_H \left( R - \frac{B}{\Delta p} \right)}$$

- Let

$$\rho_0 = P_H \left( R - \frac{B}{\Delta p} \right)$$

And

$$\rho_1 = p_H R$$

- Then

$$I \leq \frac{1}{1 - \rho_0} A$$

### Theorem

Debt/equity ratio :  $\frac{I-A}{A} \leq \frac{\rho_0}{1-\rho_0}$

## Chapter 5 The theory of Moral Hazard : An example

- It is optimal to borrow exactly  $\frac{\rho_0}{1-\rho_0}A$
- The shadow value of equity
  - $A$  gives rise to an investment equal to  $\frac{1}{1-\rho_0}A$ ,
  - and then a total return equal to  $\frac{\rho_1}{1-\rho_0}A$
  - The bank makes no profit so that  $\rho_H R_\ell = I - A = \frac{\rho_0}{1-\rho_0}A$ ,
  - So that the return on equity is :

$$\frac{\rho_1 - \rho_0}{1 - \rho_0}$$

- This is larger than 1 !

# Chapter 5 The theory of Moral Hazard : the basic Model

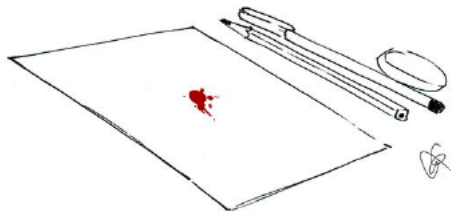


Je suis Charlie



# Je suis Charlie

Nous,  
pour faire passer nos idées,  
on n'utilise que de **l'encre.**



• SOUTIEN À •  
**CHARLIE HEBDO**

# Summary

- The **first main message** of your talk in one or two lines.
  - The **second main message** of your talk in one or two lines.
  - Perhaps a **third message**, but not more than that.
- 
- Outlook
    - What we have not done yet.
    - Even more stuff.